

Sub Title : Numerical Methods

Date : 10.04.15

Sub Code :MA6459

Branch : Civil

Duration : 3 hrs

Max.Marks:100

**PART-A (Answer all the questions)**

(10\*2=20)

1. Find the iterative formula for  $\sqrt{a}$ .
2. State the principal used in Gauss-Jordan method.
3. Find the divided difference of  $f(x)=x^3+x+2$  for the arguments 1,3,6,11
4. What is a cubic spline?
5. State three point Gaussian quadrature formula.
6. What is the order of error in trapezoidal formula?
7. State modified Euler's algorithm to solve  $y'=f(x,y)$ ,  $y(x_0)=y_0$  at  $x=x_0+h$ .
8. Write down Adam's Bashforth predictor and corrector formulae.
9. Write the diagonal five point formula for solving the two dimensional laplacian equation  $\Delta^2 u=0$ .
10. Using finite difference solve  $y''-y=0$  given  $y(0)=0, y(1)=1, n=2$

**PART-B (Answer as per choice)**

(5\*16=80)

11.a(i) Using Newton's Raphson method, find the root of  $x \log_{10} x = 1.2$ .

(8)

(ii) Apply gauss seidel method to solve the system of equations

$$20x+y-2z=17, 3x+20y-z=-18, 2x-3y+20z=25.$$

(8)

(OR)

b.(i) Using gauss-jordan method, find the inverse of the matrix  $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$

(8)

(ii) Find the dominant eigen value of  $A = \begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$  and corresponding eigen vector.

(8)

12.a(i) Given the values, find  $f(27)$  by using lagrange's interpolation

(8)

x	14	17	31	35
f(x)	68.7	64.0	44.0	39.1

(ii) Obtain the cubic spline approximation for the function  $y=f(x)$ , from the following data, given that  $y_0''=y_3''=0$

(8)

X	-1	0	1	2
Y	-1	1	3	35

(OR)

12.b(i) Using Newton's divided difference formula, find  $u(3)$  given

(8)

$$u(1)=-26, u(20)=12, u(4)=256, u(6)=844.$$

- (ii) The population of a town is as follows, find  $y(1976)$  (8)

year	1941	1951	1961	1971	1981	1991
population	20	24	29	36	46	51

- 13.a(i) Find the first, second and the third derivatives of  $f(x)$  at  $x=1.5$  if (8)

X	1.5	2.0	2.5	3.0	3.5	4.0
$f(x)$	3.375	7.000	13.625	24.000	38.875	59.000

- (ii) Evaluate  $\int_0^2 \frac{x^2+2x+1}{1+(x+1)^4} dx$  by gaussian three point formula. (8)

(OR)

- b(i) The velocity  $v$  of particle at distance  $s$  from a point on its path is given (8)

S in metre	0	10	20	30	40	50	60
V m/sec	47	58	64	65	61	52	38

Estimate the time taken to travel 60 metres by using Simpson's  $1/3^{\text{rd}}$  rule.

- (ii) Evaluate  $\int_1^{1.4} \int_2^{2.4} \frac{1}{xy} dx dy$ , using trapezoidal and Simpson's rule. (8)

- 14.a (i) Find  $y(1.2)$ , by the modified Euler's method, If  $\frac{dy}{dx} = (y-x^2)^3$ ,  $y(1)=0$  taking  $h=0.2$ . (8)

- (ii) If  $\frac{dy}{dx} = x^3 + y$ ,  $y(0)=2$ . Find  $y(0.2)$ ,  $y(0.4)$  and  $y(0.6)$  by R-K method of fourth order. (8)

(OR)

- b.(i) Using Milne's method find  $y(2)$ , if  $y(x)$  is the solution of  $\frac{dx}{dy} = \frac{1}{2}(x+y)$  given  $y(0)=2$ ,  $y(0.5)=2.636$ ,  $y(1)=3.595$  and  $y(1.5)=4.968$ . (8)

- (ii) Solve  $y' = x - y^2$ ,  $y(0)=1$  to find  $y(0.4)$  by Adam's method. Starting solutions required to be obtained using Taylor's method using the value  $h=0.1$ . (8)

- 15.a(i) By iteration method, solve the elliptic equation  $\Delta^2 u = 0$  over a square region of side 4, satisfying the boundary conditions (8)

(i)  $u(0,y)=0$  for  $0 \leq y \leq 4$

(ii)  $u(4,y)=12+y$  for  $0 \leq y \leq 4$

(iii)  $u(x,0)=3x$  for  $0 \leq x \leq 4$

(iv)  $u(x,4)=x^2$  for  $0 \leq x \leq 4$

(OR)

- b.(i) Using Crank-Nicolson's scheme, solve  $16u_t = u_{xx}$ ,  $0 < x < 1, t > 0$  subject to  $u(x,0)=0$ ,  $u(0,t)=0$  and  $u(1,t)=100t$ . Compute  $u$  for one time step, taking  $h=1/4$ . (8)

- (ii) Solve  $u_{tt} = u_{xx}$ ,  $0 < x < 1, t > 0$  subject to  $u(x,0)=100(x-x^2)$ ,  $u_t(x,0)=0$ ,  $u(0,t)=u(1,t)=0, t > 0$  by finite difference method for one time step with  $h=0.25$  (8)